# 2.2 Laws of Logarithms

# **Question Paper**

Course	CIE A Level Maths	
Section	2. Logs & Exponentials	
Topic	2.2 Laws of Logarithms	
Difficulty	Very Hard	

Time allowed: 50

Score: /40

Percentage: /100

## Question la

(a) Evaluate

$$4\log_3 729 + 3\log_2 64^2 - 3\log 100 + \ln e^6$$

[2 marks]

## Question 1b

(b) Evaluate

$$\frac{1}{2}\ln 196 + \frac{1}{3}\ln 125 + \frac{1}{4}\ln 81 + \frac{1}{5}\ln 32$$

giving your answer in the form  $\ln q$ .

[3 marks]

# Question 2

Solve the equation

$$2 \times 5^{2x+1} + 21 = 41 \times 5^x,$$

giving your answers in the form  $\log_a b$ , where a and b are rational numbers to be found.

[4 marks]



# Question 3a

Solve the following equations, giving your answers correct to 3 significant figures.

(a) 
$$8e^{3x^2-1} = 12$$

[3 marks]

# Question 3b

(b) 
$$e^{3x} - 42 = 2e^x(6e^x - 7)$$

[3 marks]

#### Question 4

Show that

$$2\log_3 x + \log_3(x^2 - 1) - 2\log_3(x + 1) \equiv \log_3 \frac{x^2(x - 1)}{(x + 1)}.$$

[3 marks]

#### Question 5

Write the following as a single logarithm

$$2\log_p(x+1) + 3\log_p(x-1) - \log_p(x^2-1).$$

[3 marks]

#### Question 6

On the same axes, sketch the graphs of  $y = e^{2x}$  and  $y = \frac{1}{2} \ln x$ .

On each graph, label any points where the graph intersects the coordinate axes.

Write down the equations of any asymptotes for each graph.

Explain the significance of the line y = x.

[5 marks]

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## Question 7

Show that  $4 - \ln 16$  can be written in the form  $4\ln(\frac{e}{2})$ .

[3 marks]

#### **Question 8**

A triangle is drawn inside a circle such that one side of the triangle is the diameter and all three vertices of the triangle lie on the circumference.

The radius of the circle is  $(3 \ln 2)$  cm.

The two smallest angles in the triangle are  $\alpha$  and  $\beta$  respectively where  $\beta = 2\alpha$ .

Find all three sides of the triangle, giving your answers in the form  $a \ln 2$ .

[5 marks]



# Question 9

How many real solutions does the equation have? Justify your answer.

$$3\log_x(x+1) = \ln e^3$$

[3 marks]

# Question 10

Without using a calculator, show that

$$\log_4 8 = \log_9 27.$$

[3 marks]

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